Transparency in Learning and Teaching

## LESS TRANSPARENT

## EXAMPLE M: SIMPLIFY EXPRESSIONS

Used by permission of Dr. Trina Palmer, Appalachian State University

Name: $\qquad$
Directions: Simplify each.
1.

$$
\frac{2 w^{2}-50}{x^{2}-4 w-5}
$$

2. $\frac{-3 w^{2}-9 w+54}{w^{2}-9 w+18}$
3. 

$$
\frac{16 v^{4} w^{2}}{12 w^{2}+20 u^{4} w}
$$

## MORE TRANSPARENT

## Revised EXAMPLE M: SIMPLIFY EXPRESSIONS

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MAT 1531 Simplification
Due: September 20

## Purpose:

The purpose of this assignment is to (1) improve your mathematical writing and (2) demonstrate your algebraic manipulation skills. This assignment will help prepare you for sim-plifying expressions from calculus and help you communicate where your understanding and misunderstanding are. Knowing how to simplify expressions is like using correct grammar -- it makes the written mathematics easier to read and understand. Real-life modeling problems are everywhere such as modeling the spread of COVID-19 or predicting future global temperatures. Simplifying the mathematical models as they are developed reduces possible errors.

Student Learning Outcomes addressed in this assignment:

1. Simplify Algebraic Expressions
2. Communicate algebraic reasoning

## Assignment:

Simplify one of the following problems, and include justifications for each manipulation.

1. $\frac{2 w^{2}-50}{\mathrm{x} 2-4 \mathrm{w}-5}$
2. $\frac{-3 w^{2}-9 w+54}{w^{2}-9 w+18}$
3. $\frac{16 v^{4} w^{2}}{12 w^{2}+20 u^{4} w}$

Sample Problem

| Simplify: $\frac{u^{2}-7 u+6}{5-5 u^{2}}$ | Answer: $\frac{-(u+7)}{5(1+u)}$ |
| :---: | :--- |
| $\frac{u^{2}-7 u+6}{5-5 u^{2}}$ | Restatement |
| $\frac{(u+7)(u-1)}{5\left(1-u^{2}\right)}$ | Factor the numerator and denominator |
| $\frac{(u+7)(u-1)}{5(1-u)(1+u)}$ | Factor the denominator (difference of two squares) |
| $\frac{-(u+7)(1-u)}{5(1-u)(1+u)}$ | Factor out a negative one in the numerator |
| $\frac{-(u+7)}{5(1+u)} * \frac{(1-u)}{(1-u)}$ | Rearrange factors (commutative property of multiplication) |
| $\frac{-(u+7)}{5(1+u)} * 1$ | $\frac{1-u}{1-u}=1$ assuming $u \neq 1$ |
| $\frac{-(u+7)}{5(1+u)}$ | Multiplicative identity |

Criteria:

|  | Proficient | Emerging | Needs Improvement |
| :--- | :--- | :--- | :--- |
| Algebraic accuracy | Includes most steps <br> and steps are <br> accurate | missing a few steps <br> and/or some steps <br> are inaccurate | many missing steps <br> and/or many <br> inaccurate steps <br> $(3)$ |
| Mathematics <br> language | reasoning is correct <br> and mostly correct <br> math language <br> (5) | reasoning is mostly <br> correct and mostly <br> correct mathematics <br> language | Much of the <br> reasoning and <br> language is incorrect <br> l(3) |

